

1. If we want to approximate

$$\sum_{n=0}^{\infty} \frac{(-1)^n}{n^3}$$

by a partial sum, how many terms are needed to get an error below  $10^{-6}$ ?

2. Label each of the following as “absolutely convergent,” “conditionally convergent but not absolutely convergent,” or “divergent.” (All sums are from  $n = 1$  to  $\infty$ .)

- (a)  $\sum (-1)^n$
- (b)  $\sum (-1)^n/n$
- (c)  $\sum (-1)^n/(n^2 + n)$
- (d)  $\sum (-1)^n/\ln(n)$
- (e)  $\sum (-1)^n e^{-n}$

3. Consider the series

$$\sum_{n=1}^{\infty} (-1)^n \sin\left(\frac{1}{n}\right)$$

A classmate makes the argument that the series converges: “This is an alternating series, and the terms of that sequence converge to 0. Thus, by the alternating series test, the series converges.”

You write a program to find the first 50 terms of the series, and the series appears to converge. Yet, when you make this argument to your TA, they stop, think for a moment, and say the following:

“The series does converge. However...”

What’s the last part of the thing they say?